

Let us start with the mortality force

```
> m := t ->
    0.0005+0.00007585775*10^(0.038*t);
```

$$m := t \rightarrow 0.0005 + 0.00007585775 \cdot 10^{(0.038 t)}$$

This is the mortality force in state 3. Note that this is before the correction was issued. You can replace it via constant 0.4 if you like.

```
> m3 := t -> 0.4*exp(0.002*t);
```

$$m3 := t \rightarrow 0.4 e^{(0.002 t)}$$

We will need the survival probability (see later)

```
> evalf(0.00007585775*10^(0.038*35) / (0.038*ln
    (10)));
```

$$0.01853534490$$

```
> p := t ->
    exp(-0.0005*t-.1853534490e-1*(10^(0.038*t)-
    1));
```

$$p := t \rightarrow e^{(-0.0005 t - 0.01853534490 (10^{(0.038 t)} - 1))}$$

Let us pretend the contract is valid for life.

```
> dsys1 :=
    {diff(v1(t), t) = (m(35+t)+0.05+0.01)*v1(t)-0.
    01*v2(t),
```

```
diff(v2(t),t)=(m(35+t)+0.03+0.05)*v2(t)-0.03*v3(t)-0.03*100000,
diff(v3(t),t)=(m3(35+t)+0.05)*v3(t)-50000,
v1(90)=0, v2(90)=0, v3(90)=0 };
```

```
dsys1 := { v3(90) = 0, v1(90) = 0, v2(90) = 0,  $\frac{d}{dt}v1(t) =$ 
 $(0.0605 + 0.00007585775 \cdot 10^{(1.330 + 0.038 t)}) v1(t) - 0.01 v2(t),$ 
 $\frac{d}{dt}v2(t) = (0.0805 + 0.00007585775 \cdot 10^{(1.330 + 0.038 t)}) v2(t)$ 
 $- 0.03 v3(t) - 3000.00,$ 
 $\frac{d}{dt}v3(t) = (0.4 e^{(0.070 + 0.002 t)} + 0.05) v3(t) - 50000 }$ 
```

```
> dsol1 := dsolve(dsys1, numeric, range =
0..90);
```

```
dsol1 := proc(x_rkf45) ... end proc
```

```
> dsol1(0);
```

```
[t = 0., v1(t) = 8875.76513937075652,
v2(t) = 69588.8967815554060, v3(t) = 103995.793231547912]
```

The reserves calculated are correct for states 2 and 3. Let us now amend the value at time 0 for state 1 (see class for explanation) to take into account the fact that the contract is terminated at time 25 if at state 1.

```
> evalf (p (25) *exp (-0.06*25)) ;
```

```
0.1902985564
```

```
> dsol1 (25) ;
```

```
[t = 25., v1(t) = 4395.57887371197102,
```

```
v2(t) = 52228.1348577902245, v3(t) = 99444.4052801718062]
```

so the up front premium is

```
> evalf (8875.76513937075652 - .1902985564*4395.57887371197102) ;
```

```
8039.292825
```

Now the reserves at time 10 for the life contract

```
> dsol1 (10) ;
```

```
[t = 10., v1(t) = 7255.82044133415458,
```

```
v2(t) = 64526.0298765843182, v3(t) = 102153.606377629825]
```

Again the values for states 2 and 3 are correct. To amend the value for state 1 let us first calculate the survival probability for a 45 year old.

```
> evalf (0.00007585775*10^(0.038*45) / (0.038*ln(10))) ;
```

```
0.04446319552
```

```
> p45 := t ->
```

```
exp (-0.0005*t - .4446319552e-1*(10^(0.038*t) - 1)) ;
```

```
p45 := t → e(-0.0005 t - 0.04446319552 (10(0.038 t) - 1))
```

And here follows the adjustment which will give 5683.79 as the premium.

```
> evalf(p45(15)*exp(-0.06*15));
```

0.3576382637

```
> evalf(7255.82044133415458-.3576382637*4395.  
57887371197102);
```

5683.793245

Finally note that the premium for a 45 year old in state 2 is of course 64526.03