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# From thesis to trading: a trend detection strategy

#### DB Quantitative Strategy – FX & Commodities March 2011



Deutsche Bank AG/London

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A Passion to Perform.



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## Introduction (1)

- Quantitative strategy is about applying mathematical techniques to understand and predict financial market dynamics.
- Less macroeconomics, more statistics. Understanding the patterns in the information. Major focus on speed and dependency, not just direction.
- Once we feel comfortable in our understanding, and in the stability of these patterns, we employ them in building systematic trading strategies in spot and derivatives accross different asset classes.



## **Introduction (2)**

- Most of the work is about building and implementing systematic trading models.
- The clientelle is divided into 2 constituencies:
  - Internal: implement models at given proprietary books, supervised by trading desks
  - External: educational roadshows with a variety of the bank's clients
- We run an annual internship programme, and the models often result from the work of our interns.
- When the intern is an MSc or PhD student, we try to link the topic with the intern's thesis.
- Florent Robert: intern since July 2010. Idea: employ innovative techniques to identify regime switches in the data. Eventually settled for techniques that can be implemented in data other than just volatility. The work culminated in a fullyimplementable momentum strategy.

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#### The theory (1) Motivation

- Markovian regime switching to model
  - Switches in volatility
  - Credit defaults
- Bayesian disorder detection to model regime switches in prices
  - More straightforward, no transition matrix
  - Fair assumption: FX prices can be modelled locally as Brownian motions







- Detect as quickly as possible a change in the observable system's behaviour. Time at which the change occurs: T, the change-point.
- Here change in the system behaviour = change in the drift: from 0 to  $\vartheta$  at  $\tau$
- T is the stopping rule, the time of the alarm. We want to minimize the expected miss
- Introducing, the a posteriori probability process  $\prod_t$ : probability that regime change has already occurred by time t, given the observations available up to that time **Deutsche Bank**

#### The theory (3) Thesis

- Approach using Girsanov: from new measure to actual measure
  - New measure  $(\Omega, \mathcal{F}, \mathbb{P}_0)$ :
    - $X_t$  is a Brownian motion independent from  $\tau$
  - Larger filtration  $\mathcal{G}_t := \sigma(\tau, \hat{X}_s; 0 \le s \le t)$  Change using  $Y_t = \frac{\vartheta}{\sigma} \mathbf{1}_{\{\tau \le t\}}$

$$\begin{aligned} \left. \frac{d\mathbb{P}}{d\mathbb{P}_0} \right|_{\mathcal{G}_t} &= \exp\left(\int_0^T Y_s d\hat{X}_s - \frac{1}{2} \int_0^T |Y_s|^2 ds\right) \\ &= \frac{L_t}{L_\tau} \cdot \mathbf{1}_{\{\tau \le t\}} + \mathbf{1}_{\{\tau > t\}} := Z_t \end{aligned}$$

- Exponential likelihood ratio process  $L_t := \exp\left(\frac{\vartheta}{\sigma}\hat{X}_t \frac{\vartheta^2}{2\sigma^2}t\right)$
- In the newly defined measure  $(\Omega, \mathcal{F}, \mathbb{P})$ , we have exactly the problem that we originally posited

#### The theory (4) Thesis

- **Theory Bayes rule:**  $\Pi_t := \mathbb{P}[\tau \le t | \mathcal{F}_t] = \frac{\mathbb{E}_0 \left[ Z_t \mathbf{1}_{\{\tau \le s\}} | \mathcal{F}_t \right]}{\mathbb{E}_0 \left[ Z_t | \mathcal{F}_t \right]}$   $\Pi_t = \frac{p L_t + (1-p) \int_0^t (L_t/L_s) \cdot \lambda e^{-\lambda s} ds}{p L_t + (1-p) \int_0^t (L_t/L_s) \cdot \lambda e^{-\lambda s} ds + (1-p) e^{-\lambda t}}$
- More interested in the dynamics of  $\Pi_t$ . Innovations process
  - Using Levy theorem, *B* is a Brownian motion in  $(\Omega, \mathcal{F}, \mathbb{P})$

$$B_{t} = \frac{1}{\sigma} X_{t} - \frac{\vartheta}{\sigma} \int_{0}^{t} \Pi_{s} ds$$
  
Ito's theorem,  $\Phi_{t} = \frac{\Pi_{t}}{1 - \Pi_{t}}$ 
$$d\Pi_{t} = \lambda \left(1 - \Pi_{t}\right) dt + \frac{\vartheta}{\sigma} \Pi_{t} \left(1 - \Pi_{t}\right) dB_{t}$$



# The theory (5) Thesis $\lambda (1-x) Q'(x) + \frac{1}{2} \left(\frac{\vartheta}{\sigma}\right)^2 x^2 (1-x)^2 Q''(x) = \frac{1}{2} - x; \text{ for } 0 < x < p_*$ $\lambda (1-x) Q'(x) + \frac{1}{2} \left(\frac{\vartheta}{\sigma}\right)^2 x^2 (1-x)^2 Q''(x) \ge \frac{1}{2} - x; \text{ for } p_* < x < 1$ Finding the optimal stopping rule $Q(x) \le 0; \text{ for } 0 \le x < p_*$ $Q(x) = 0: \text{ for } p_* \le x \le 1.$

- If you can find such a function Q, then applying Ito to  $Q(\Pi)$ , you can show that  $\mathbb{E}\left[\int_{0}^{T} \left(\Pi_{t} \frac{1}{2}\right) dt\right] \ge Q(p) \mathbb{E}\left[Q(\Pi_{t})\right] \ge Q(p)$
- Remember that  $\mathcal{R}(T) = \mathbb{E}(\tau) + 2 \cdot \mathbb{E} \int_{-T}^{T} \left( \Pi_t \frac{1}{2} \right) dt$ . Is there a stopping rule  $T_*$  such that  $\mathbb{E} \left[ \int_{0}^{T_*} \left( \Pi_t \frac{1}{2} \right) dt \right] = Q(p)$

We can achieve this by taking  $T_* = \inf \{t \ge 0 | \Pi_t \ge p_*\}$ 

Showing that Q exists, we get  $P_*$  and then

$$T_* = \inf\left\{t \ge 0 | \frac{p}{1-p} + \lambda \int_0^t e^{-\frac{\vartheta}{\sigma^2}X_s + \left(\frac{\vartheta^2}{2\sigma^2} - \lambda\right)s} ds \ge \frac{p_*}{1-p_*} e^{-\frac{\vartheta}{\sigma^2}X_t + \left(\frac{\vartheta^2}{2\sigma^2} - \lambda\right)t}\right\} \blacksquare$$

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• Implementation, marketing, internships



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#### From thesis to trading model (1) How can it be implemented?

- The idea is novel: it employs unusual but powerful techniques to detect switches between 3 market states, a clear improvement from traditional price action models (which focus on 2 market states)
- The clearest application is to a momentum strategy: to be long in an up-trend, short in a down-trend, and neutral in a sideways state
- In adapting to a trading model, a few assumptions must be made:
  - Exchange rate price changes can be *locally* normally distributed
  - The structure of the model does not alter much when evaluated in discrete time



#### From thesis to trading model (2) Estimating parameters: a modified validation approach

- What needs to be optimised?
  - The template distributions: first and second moments according to the slope (gradient) of the trend, and the variability around that slope through time. This underpins our assumption of local normality.
  - The switch mechanism: trend length, and thus the way that a trend switch becomes more likely through time. We assume the length of each trend follows a geometric distribution with an individual parameter. In other words, the likelihood of a trend switch rises with time in non-linear fashion.



#### From thesis to trading model (3) Estimating parameters: a modified validation approach





#### From thesis to trading model (4) Validation: a sequence of training vs out-of-sample windows

- Backtest, not simulation
  - Simulation: estimate the future based on today. Popular among pricing models. Forward-looking information (option prices) is used in calibrating the parameters of a process under a pricing measure. These are then applied to simulate the likely paths of the process in the future and thus to calculate the present value of an exotic payoff.
  - Backtest: evaluate the historical performance. The procedure will fit the required parameters to historical data to identify what best fits the purpose.
  - Simulation uses forward-looking data to estimate value: likely trajectory, then current price. Backtests use past information to estimate value: patterns, stability and then trading decisions. Backtests evaluate goodness of fit, a key component of trading strategies based on statistical convergence.In most of our models, we calibrate parameters based on backtests.

#### From thesis to trading model (5) Validation: a sequence of training vs out-of-sample windows

- Overfitting: dangers of backtesting
  - In-sample vs out-of-sample treatment
- Modified K-fold cross-validation: cut the data into smaller in-sample and out-of-sample windows, and use data to train and test.
- Optimise parameters in-sample according to risk-adjusted performance.
- Evaluate performance out-of-sample; in a good model, the in-sample performance is generally a good predictor of out-of-sample returns.



Note: the dotted channel represents the actual (out-of-sample) trading period. The strategy's cumulative P&L results from the sum of the OS segments. Source: Deutsche Bank





#### From thesis to trading model (6) Stability and operational risks

- K-fold window choice: robustness vs adaptability
- Stability: what happens to your equity curve if you bump the data?
- Operational reality: what happens to your equity curve if you bump transaction costs and execution time?



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#### Results (1) Positive aspects

- The results for EUR/USD are positive and linear.
- Intra-hour frequencies are noisier, and produce less trends; lower frequencies do better.
- Individual returns are somewhat similar to traditional momentum: low hit ratios (~50%) but high positive-to-negative trade returns ratio.
- More linearly consistent returns compared to a standard technical analysis strategy.
- Combining individual frequencies gives better returns. The model addresses shorter and longer trends.
- Positive and asymmetric correlation to EUR/USD implied volatility.





#### **Results (2)** Positive aspects





#### **Results (3)** Risks and future work

- Are we capturing enough information by fitting a state into 2 parameters?
- The model assumes trades can be executed at any time of the day. Is that realistic? What are the implications of execution delay?
- Does it really perform better than a simpler MACD strategy?
- Is this the best way to implement a price action switch model?





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#### What next?

- Internal implementation
- Follow-up research notes
- Educational roadshows

What model will come next? Global

Macro

**Global Markets Research** 

14 February 2011

#### **FX Special Reports** Gaining Momentum

#### Modelling price action

This report introduces a model that "learns" about different price action states, and uses that information to identify trends and detect switches in the future. The results of a momentum strategy based on the model outperform a standard technical analysis strategy, and imply an asymmetric correlation to vol.

#### Learning, detecting and switching between price action states

- Price action strategies are very popular in foreign exchange, and typically divided into the momentum and mean-reversion styles.
- We introduce a model that addresses both styles. Our model "learns" about the characteristics of an uptrend, a down-trend and sideways price action for an underlying asset.
- We use this knowledge to identify the current price action state, and apply specific algorithms to detect changes from one regime to another. The algorithms utilise Bayesian disorder detection, and a sequential regimeswitching tool.
- We create a simple momentum strategy based on the model, highlighting its performance when applied to EUR/USD. The backtest shows strong returns over time, outperforming a standard technical analysis strategy and implying an asymmetric correlation to volatility.





## Internships in FX & Commodity Quant Strategy

- Opportunity to join a team ranked as:
  - #1 in FX Quantitative Strategy by the Euromoney Survey (2009, 2010)
  - #1 in Derivatives Research by the Risk Awards Survey (2011)
  - Top 3 Commodities Research team by Energy Risk (2011)
- Opportunity to join a bank ranked as:
  - #1 in Foreign Exchange by the Euromoney Survey (past 6 years)
  - #1 in Commodity Derivatives by IFR (2011)
- Looking to hire 1-2 interns
- Preference for 1-year internships, but flexible duration and flexible start date
- Looking for candidates with strong quantitative and computing skills
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